

# Introduction to ODS Testing & Experimental Modal Analysis

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# Topics of this Presentation

- What *makes things vibrate?*
  - First Law of Modal Analysis (1<sup>st</sup> LoMA): *Any object with mass & elasticity will vibrate*
  - Second Law of Modal Analysis (2<sup>nd</sup> LoMA): *Forces cause vibration*
  - Third Law of Modal Analysis (3<sup>rd</sup> LoMA): *All vibration is a summation of mode shapes*
  - Fourth Law of Modal Analysis (4<sup>th</sup> LoMA): *All modes are excited at all frequencies*
- How is *mechanical vibration defined?*
- What is *an ODS?*
- What is *a Mode Shape?*

# Mechanical Engineering Considerations

	No Forces	Forces
No Motion	Styling	Statics
Motion	Kinematics	<i>Dynamics</i>



Styling



Statics



Kinematics

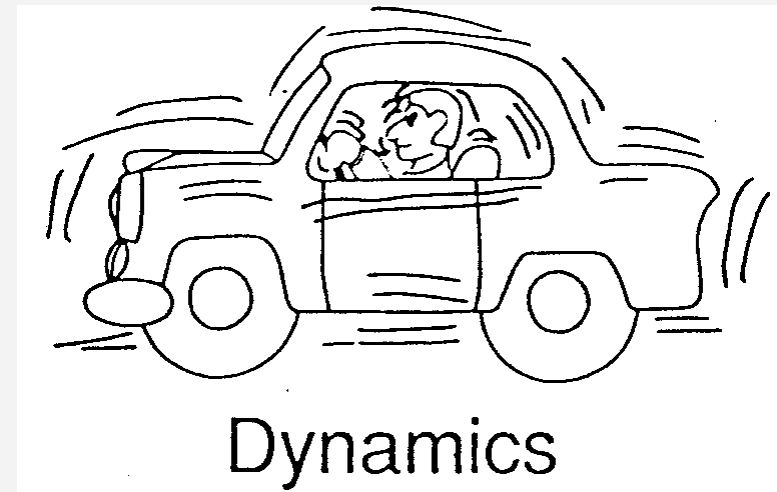


Dynamics

# Why Is Vibration Analysis Needed?

A Machine or Structure can have one or more of the following ***vibration-related problems***

- 1. Difficult to control***
- 2. Makes too much noise***
- 3. Cannot maintain tolerances***
- 4. Wears out too fast***
- 5. Fatigues prematurely***
- 6. Fails unexpectedly***



# Two Types of Vibration

- First Law of Modal Analysis (1<sup>st</sup> LoMA): *Any object with mass & elasticity will vibrate*
- Second Law of Modal Analysis (2<sup>nd</sup> LoMA): *Forces cause vibration*

**Forced Vibration:** Internal or external forces which *cause rigid body motion*

**Resonant Vibration:** Internal or external forces which *excite one or more resonances*

# Resonant Vibration

- First Law of Modal Analysis (1<sup>st</sup> LoMA): *Any object with mass & elasticity will resonate*
- Second Law of Modal Analysis (2<sup>nd</sup> LoMA): *Forces cause vibration*

***All vibration*** is Forced vibration

*All resonances participate* in Forced vibration

**Spatial descriptions of vibration**

Forced vibration => Operating Deflection Shape (ODS)

Resonant vibration => Mode Shape

# What is an Operating Deflection Shape (ODS)?

- An ODS is a *spatial description of the deformation* of a machine or structure
- A *time-based ODS* changes over time
- A *frequency-based ODS* changes with frequency
- An *order-based ODS* changes with machine speed  
(order => a *multiple of the running speed*)

# An ODS Helps Answer the Following Questions

- What is the *motion of one point relative to another?*
- Where is a *machine moving the most?*
- *How much* is a machine moving? (IPS < 1.0?)
- *Is a resonance participating* in the response?
- Is there *structure-born noise source?*
- Do corrective actions *reduce noise or vibration levels?*



# What is a Mode of Vibration?

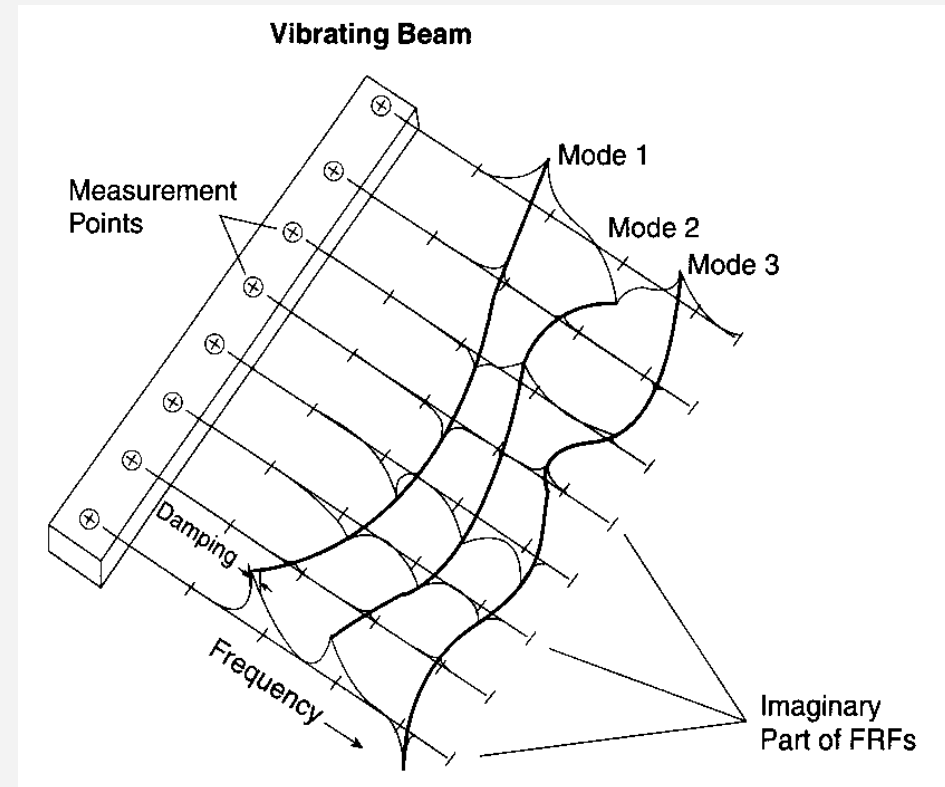
- A mode of vibration is a *mathematical representation of a structural resonance*
- When *dynamic forces are applied*, and *energy is trapped* within the boundaries of a structure, *it will resonate*
- When energy is trapped within the boundaries of a structure, it causes a *standing wave deformation*, which is called *a mode shape*
- A structure *will resonate* when its modes *readily absorb energy*
- A structural resonance can be thought of as a *mechanical amplifier* (A *small dynamic load* can cause *excessive deformation*)

# Modal Parameters From FRFs

- Third Law of Modal Analysis (3<sup>rd</sup> LoMA): *All vibration is a summation of mode shapes*
- Fourth Law of Modal Analysis (4<sup>th</sup> LoMA): *All modes are excited at all frequencies*

➤ Each mode is *defined by three parameters*

- Modal frequency  
(*natural frequency* of a resonance peak)
- Modal damping  
(*width* of a resonance peak)
- Mode shape  
(*magnitude & phase* of a resonance peak at the same frequency)



# Trapped Energy Causes Resonant Vibration?

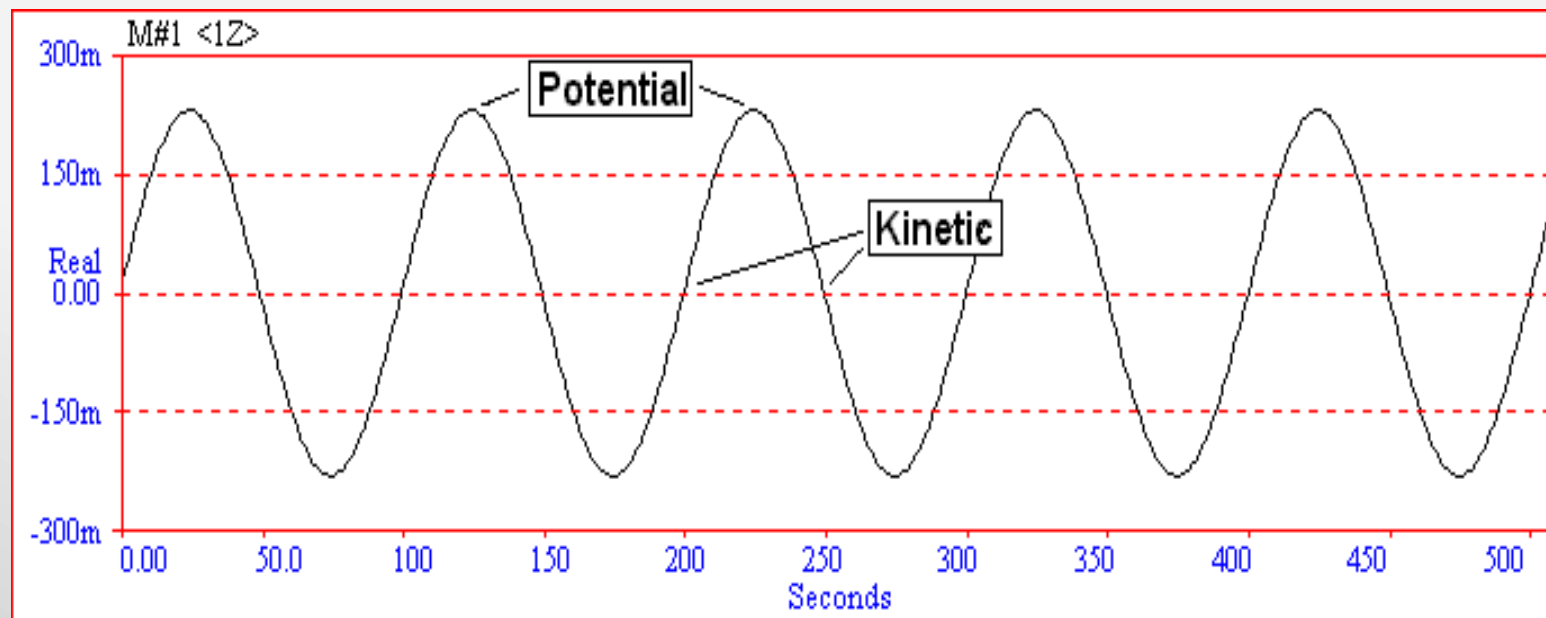
- First Law of Modal Analysis (1<sup>st</sup> LoMA): *Any object with mass & elasticity will vibrate*
- Second Law of Modal Analysis (2<sup>nd</sup> LoMA): *Forces cause vibration*
- Resonant vibration is caused when *Energy* is,
  - 1) *Trapped within the boundaries* of a structure
  - 2) *Moves freely within the structural material*
  - 3) *Cannot readily escape*
- *Striking a bell* causes it to resonate
- *Striking a sandbag* will not cause it to resonate



# What Happens To Trapped Energy?

- First Law of Modal Analysis (1<sup>st</sup> LoMA): *Any object with mass & elasticity will vibrate*
- Second Law of Modal Analysis (2<sup>nd</sup> LoMA): *Forces cause vibration*

Trapped energy is converted between *potential & kinetic energy* within a structure



# What Happens To Trapped Energy?

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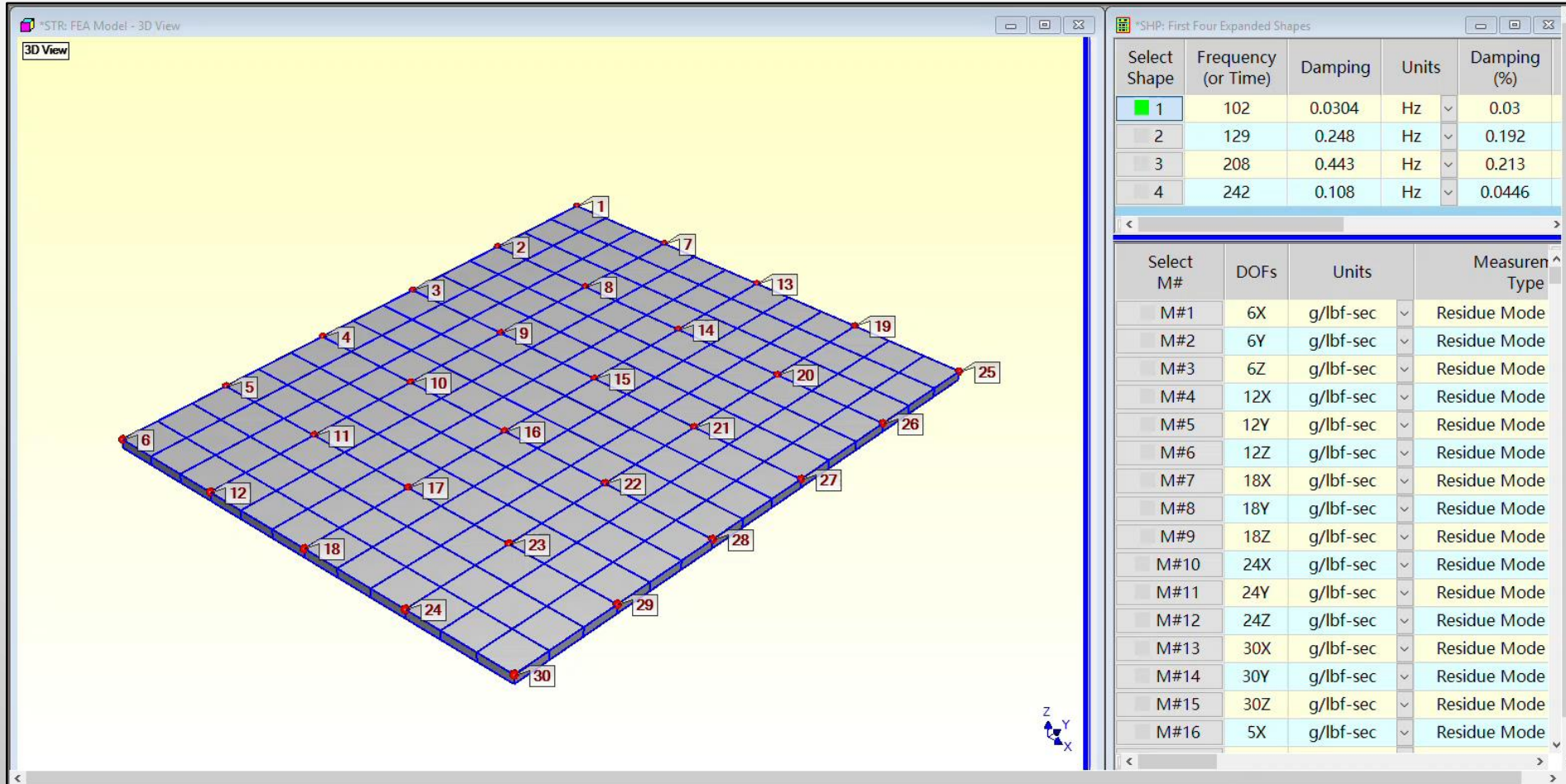
$$\mathbf{M} \ddot{\mathbf{x}}(t) + \mathbf{K} \mathbf{x}(t) = \mathbf{0}$$

$$\text{Inertia} + \text{Stiffness} = 0$$

- Trapped energy is exchanged between the *mass & elastic properties* in a structure
- The *mass (inertial) & elastic (stiffness)* forces are always *equal & opposite* to one another

# What Does Resonant Vibration Look Like?

- Trapped energy causes *standing wave deformations* at *specific natural frequencies*
- These *standing waves* are called *mode shapes*

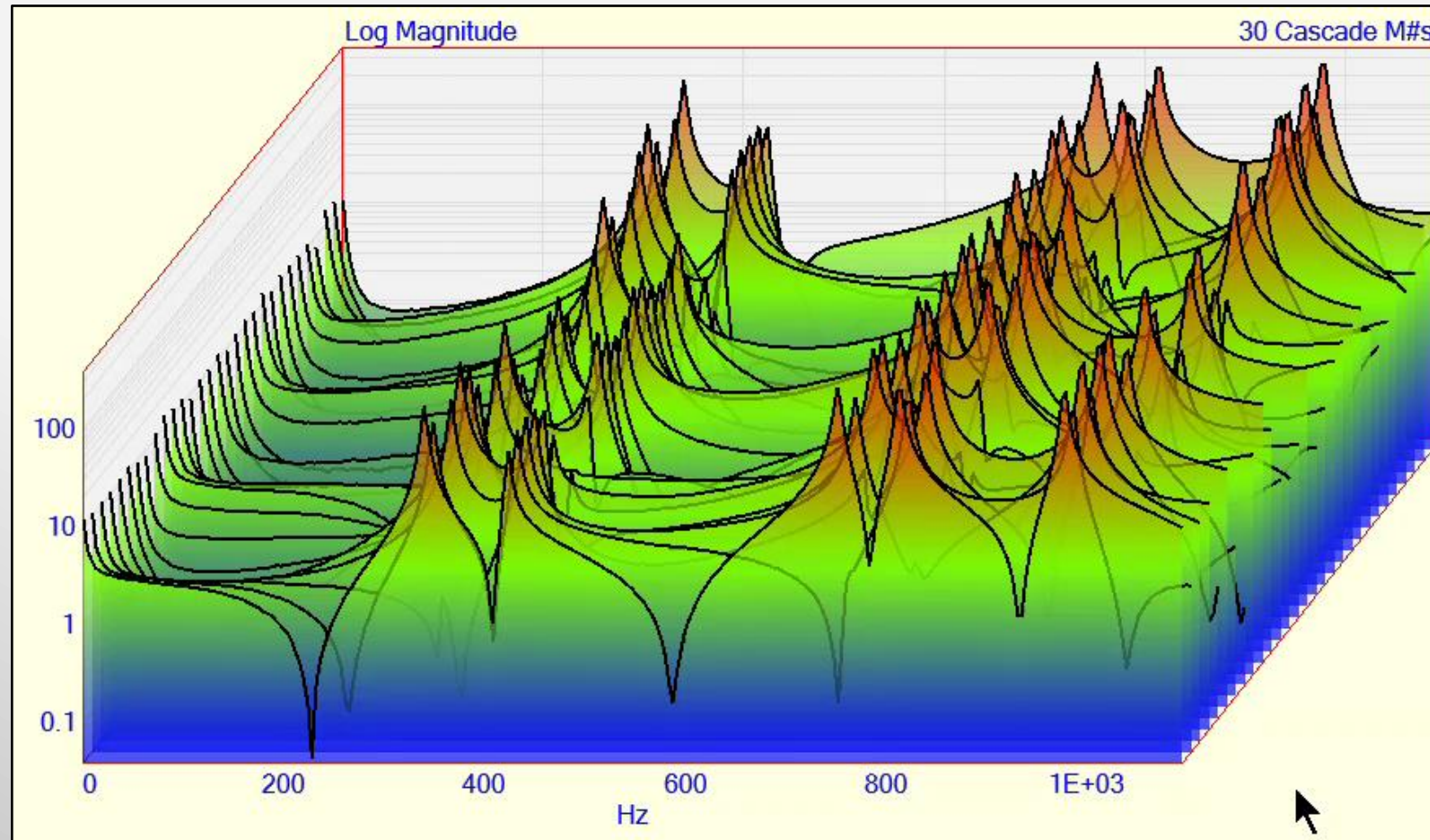


Video



# Resonances Are Dangerous!

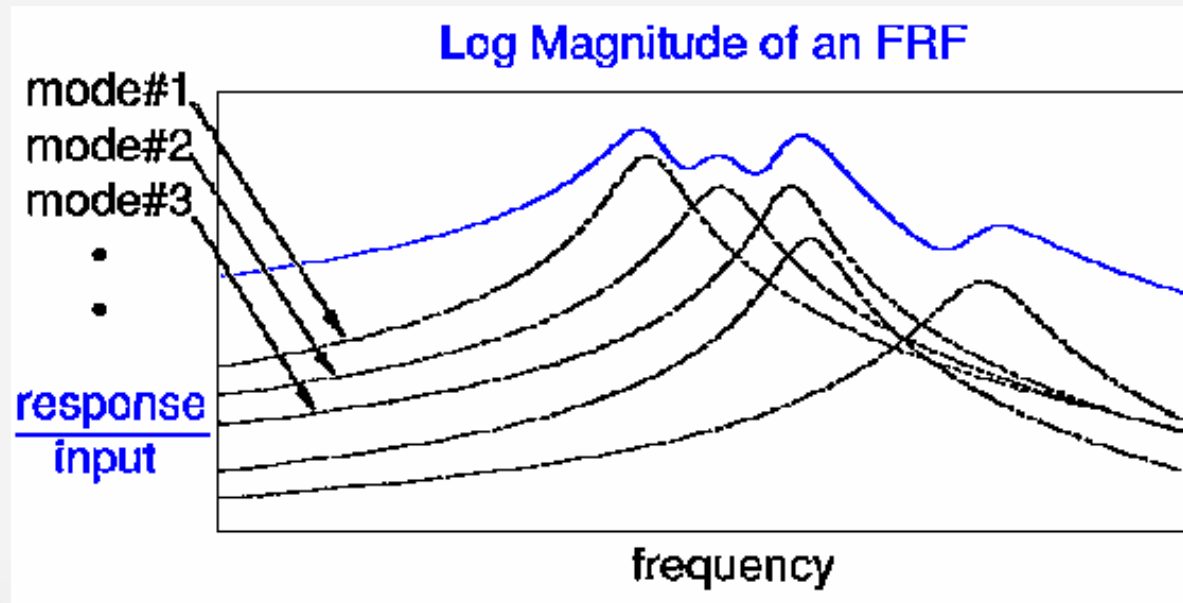
- Resonances act as *Mechanical Amplifiers*
- Energy input *at or near a natural frequency is easily absorbed*, resulting in *high amplitude vibration*



[Video](#)

# All Vibration is a *Summation* of Resonance Curves

- Third Law of Modal Analysis (3<sup>rd</sup> LoMA): *All vibration is a summation of mode shapes*
- Fourth Law of Modal Analysis (4<sup>th</sup> LoMA): *All modes are excited at all frequencies*



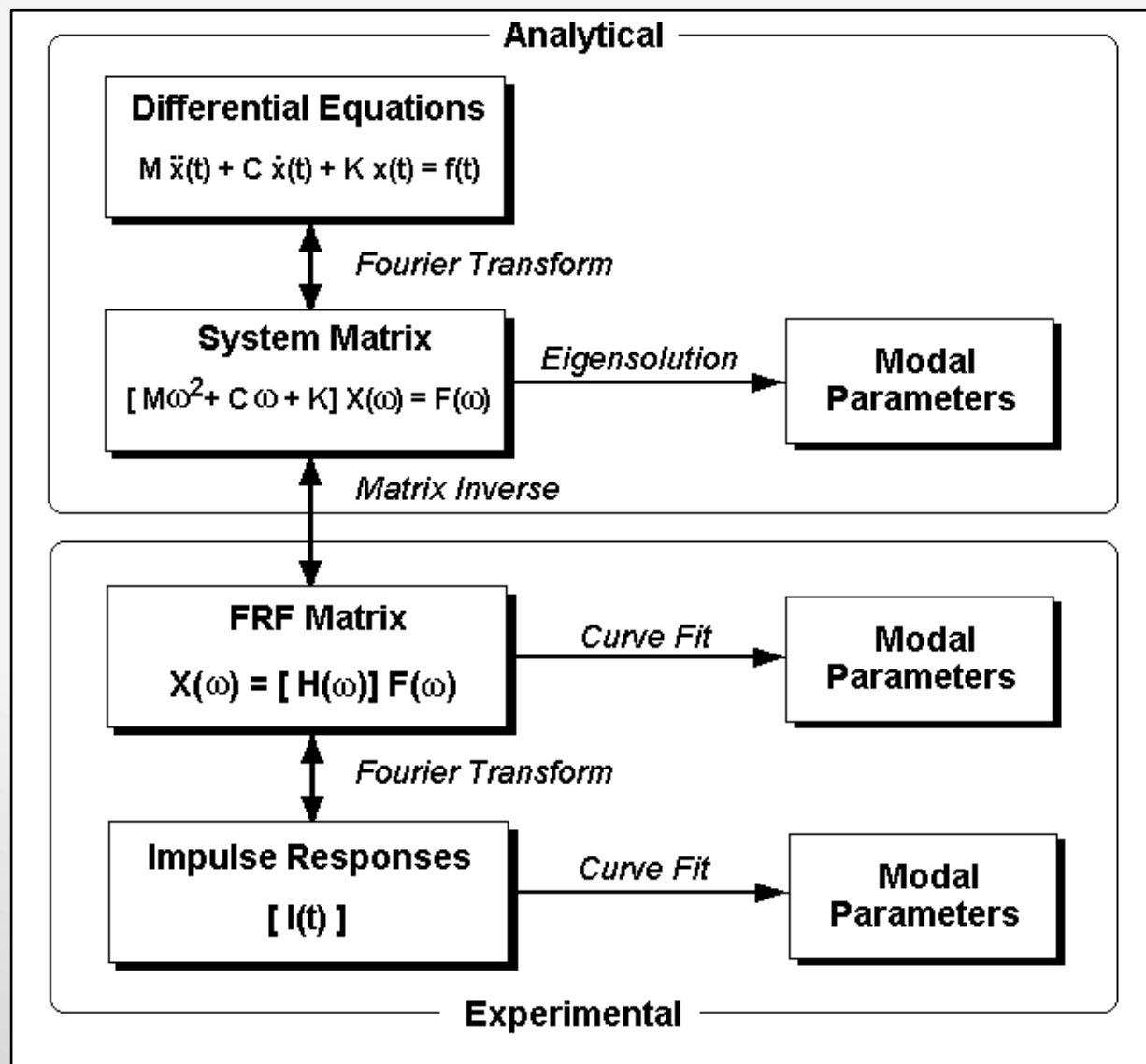
- The *FFT* transforms each time waveform into its corresponding *Digital Fourier Transform (DFT)*, *without loss of information*
- *Auto spectra, Cross spectra, Transmissibility's, FRFs, & ODS-FRFS* are calculated from *DFTs*
- Each *resonance curve corresponds to a mode of vibration*



# Two Ways to Obtain Mode Shapes

- **Experimental Modal Analysis (EMA):** EMA mode shapes are extracted from experimentally derived *time waveforms* or *frequency waveforms* that *characterize the structural dynamics*
- **Finite Element Analysis (FEA):** FEA mode shapes are obtained as solutions to a set of *differential equations* that *characterize the structural dynamics*
- **Both EMA & FEA** are based upon the *Laws of Modal Analysis (LoMA)*

# Two Ways to Obtain Mode Shapes



# Uses of Experimental Modal Analysis (EMA)

## Product Test & Measurement

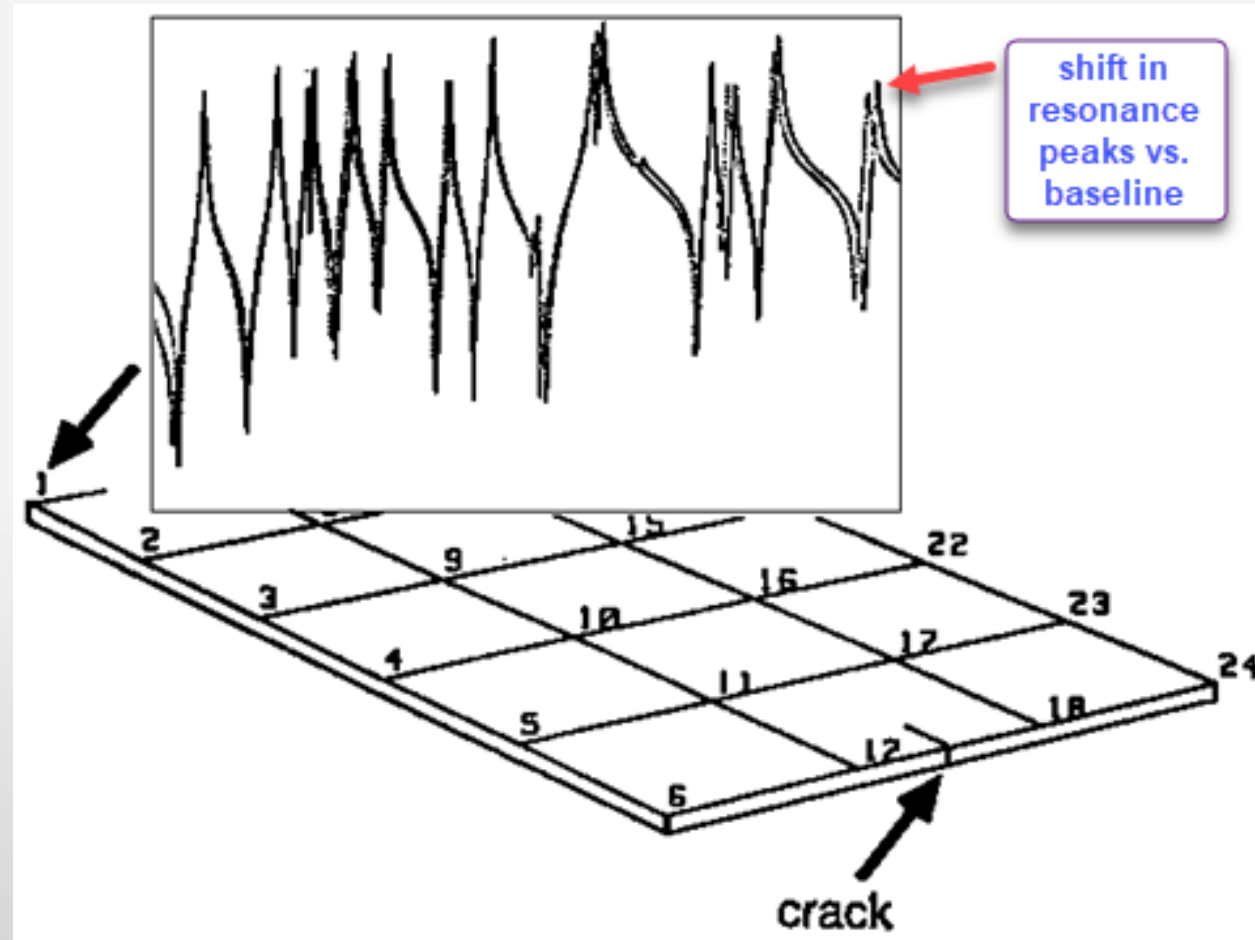
- Trouble Shooting
- FEA Model Verification
- FEA Model Updating
- Dynamics Simulation
- Dynamics Modification

## Machinery Maintenance Structural Health Monitoring

- Trouble Shooting
- Route-Based Monitoring
- In-Situ Monitoring
- New Installation Qualification
- Post-Maintenance Verification
- Fault Diagnostics

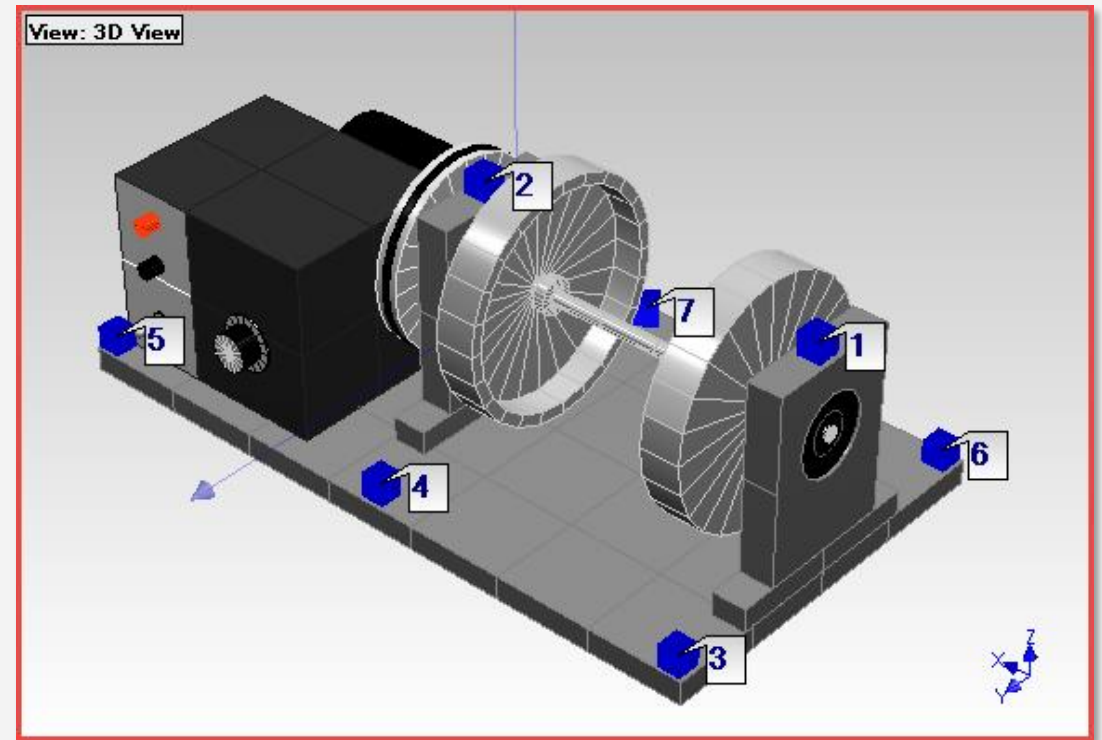
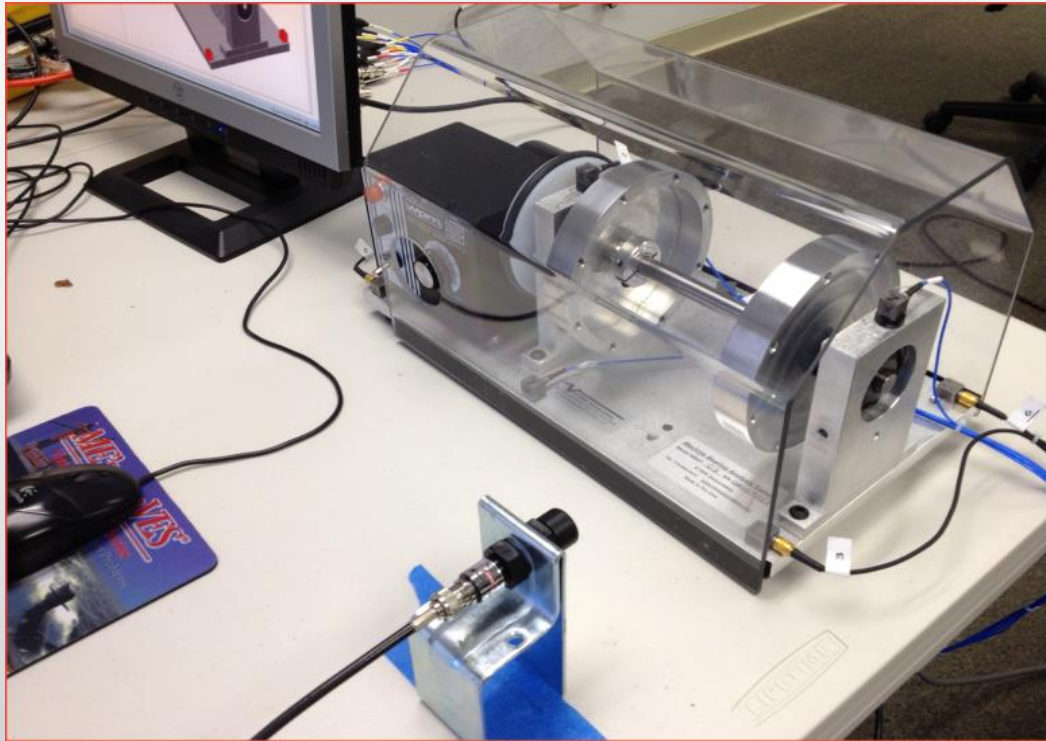
# Modes Are Sensitive Indicators Of Physical Changes

Physical damage will cause a *shift in the modal frequencies* of a machine or structure



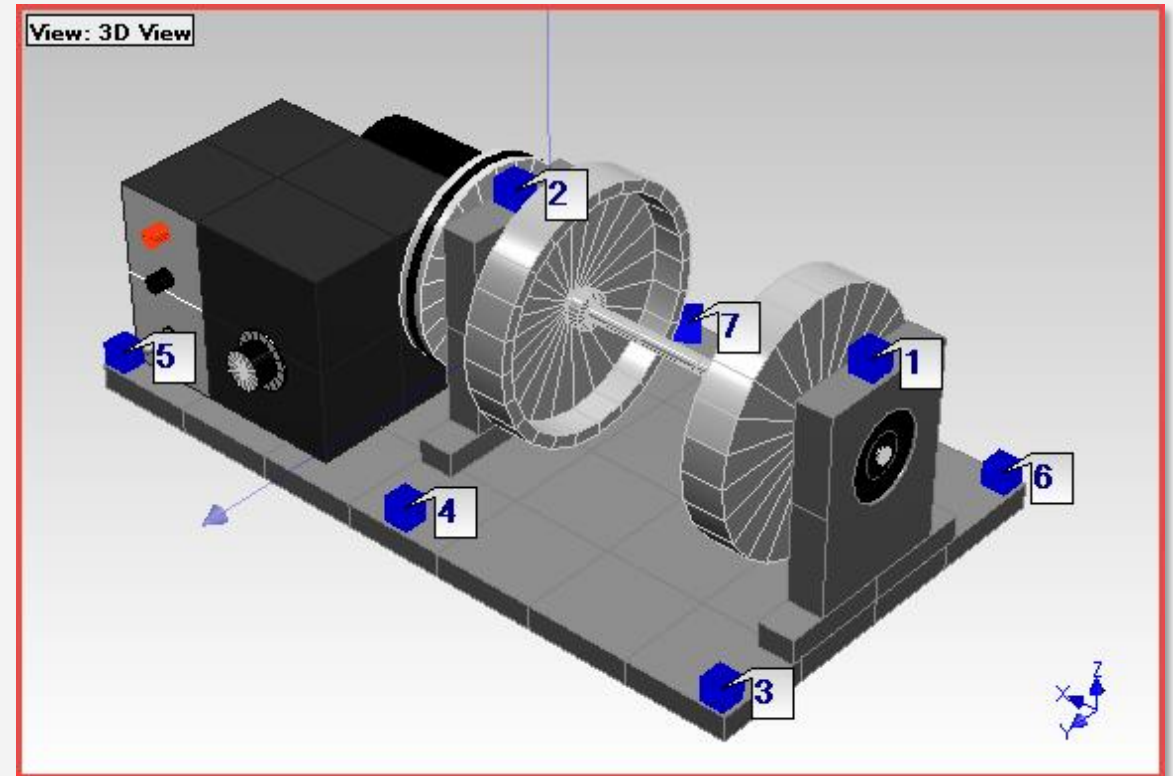
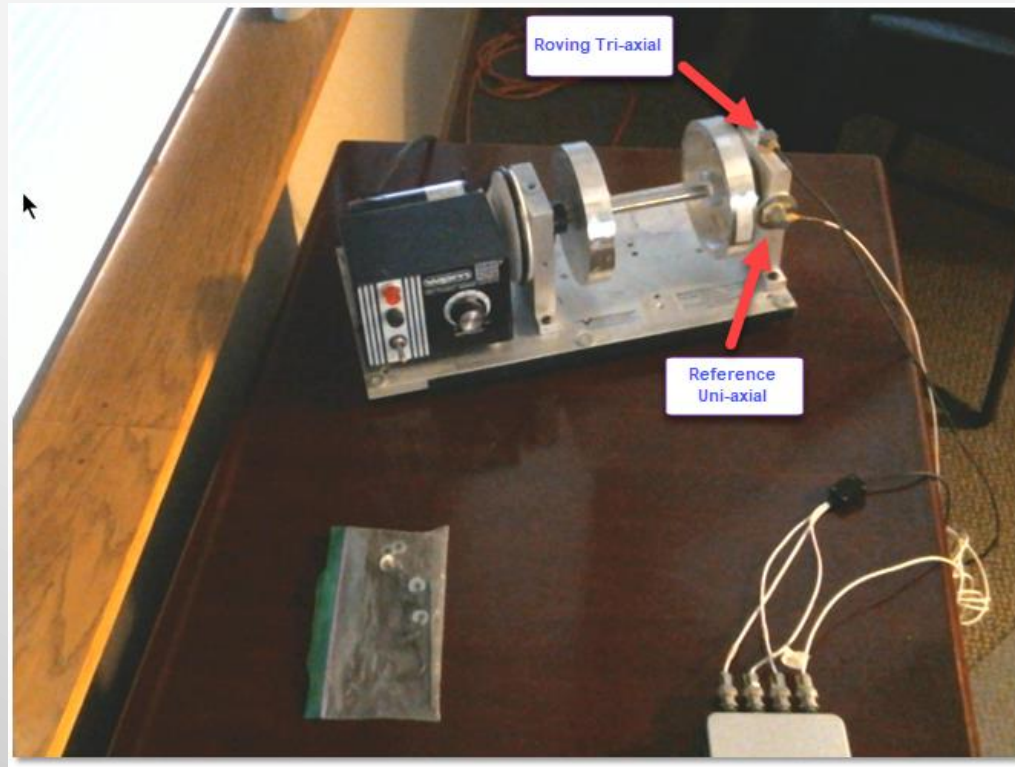
# Operating Deflection Shapes Using 24-Channel Acquisition

During operation of this rotating machine, data was acquired at eight locations using *eight tri-axial accelerometers* and *24-channel simultaneous data acquisition*



# Operating Deflection Shapes Using 4-Channel Acquisition

During operation of this rotating machine, data was also acquired at *eight locations* using a *fixed uni-axial*, a *roving tri-axial accelerometer* and a *4-channel simultaneous acquisition*

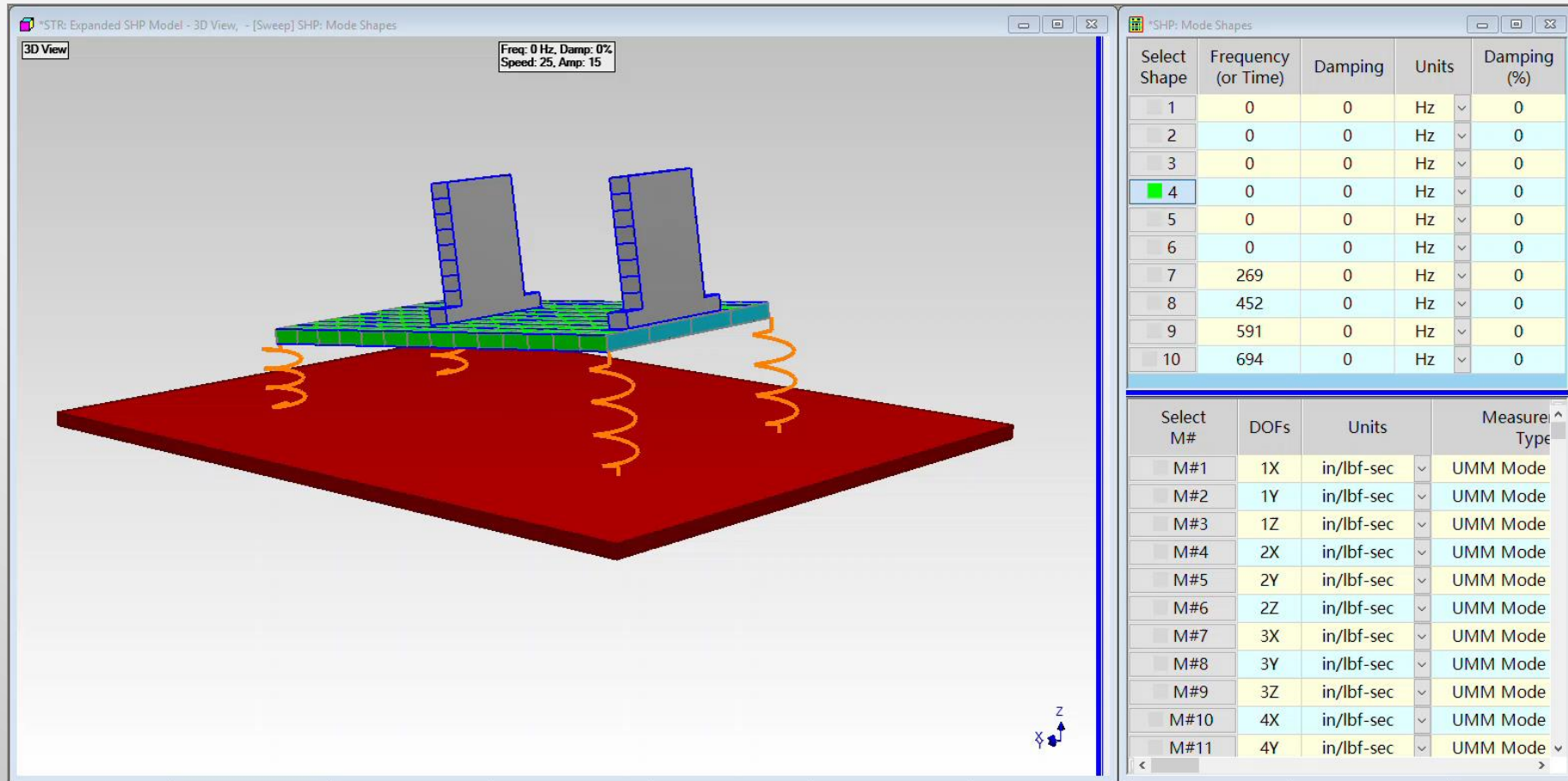




# Mode Shapes of the Base Plate & Bearing Blocks

### Third Law of Modal Analysis (3<sup>rd</sup> LoMA): *All vibration is a summation of mode shapes*

**Six Rigid Body and four Flexible Body mode shapes describe *most of the dynamics* of the machine**

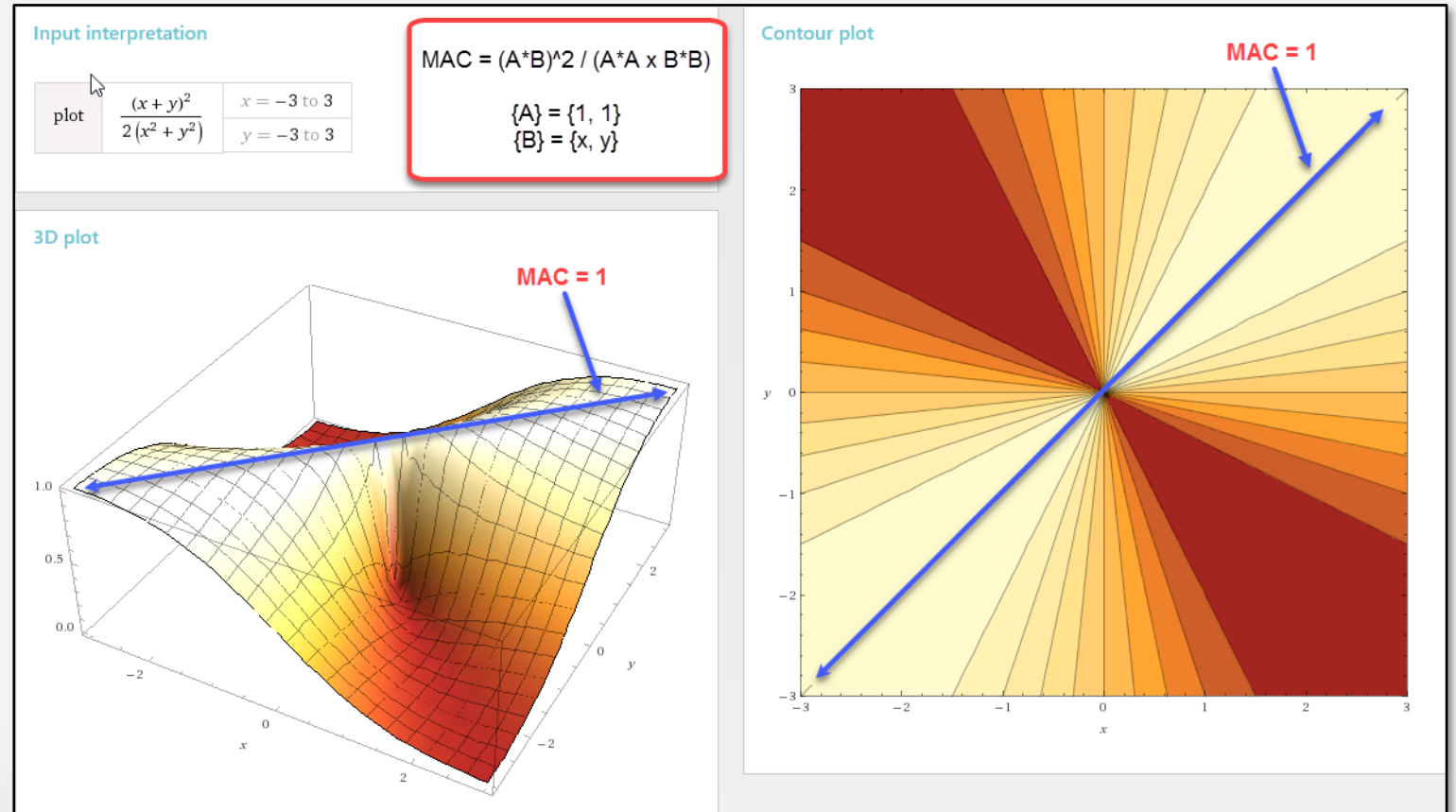


## Video

# Modal Assurance Criterion (MAC)

*Numerical comparison between two shapes*

- **MAC = 1** ➔ two shapes are *co-linear*
- **MAC > 0.9** ➔ *almost co-linear*
- **MAC < 0.9** ➔ *not co-linear*

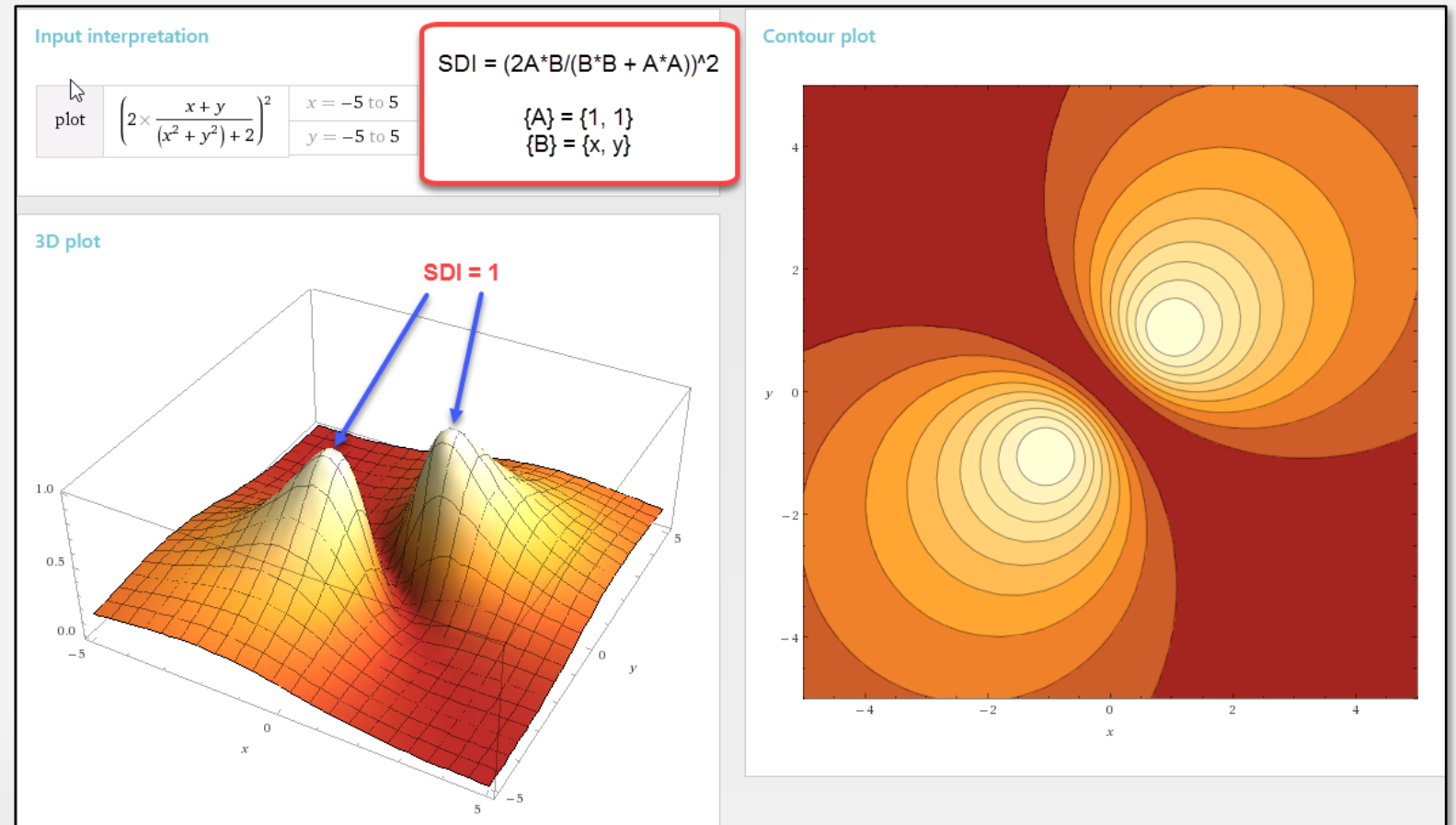




# Shape Difference Indicator (SDI)

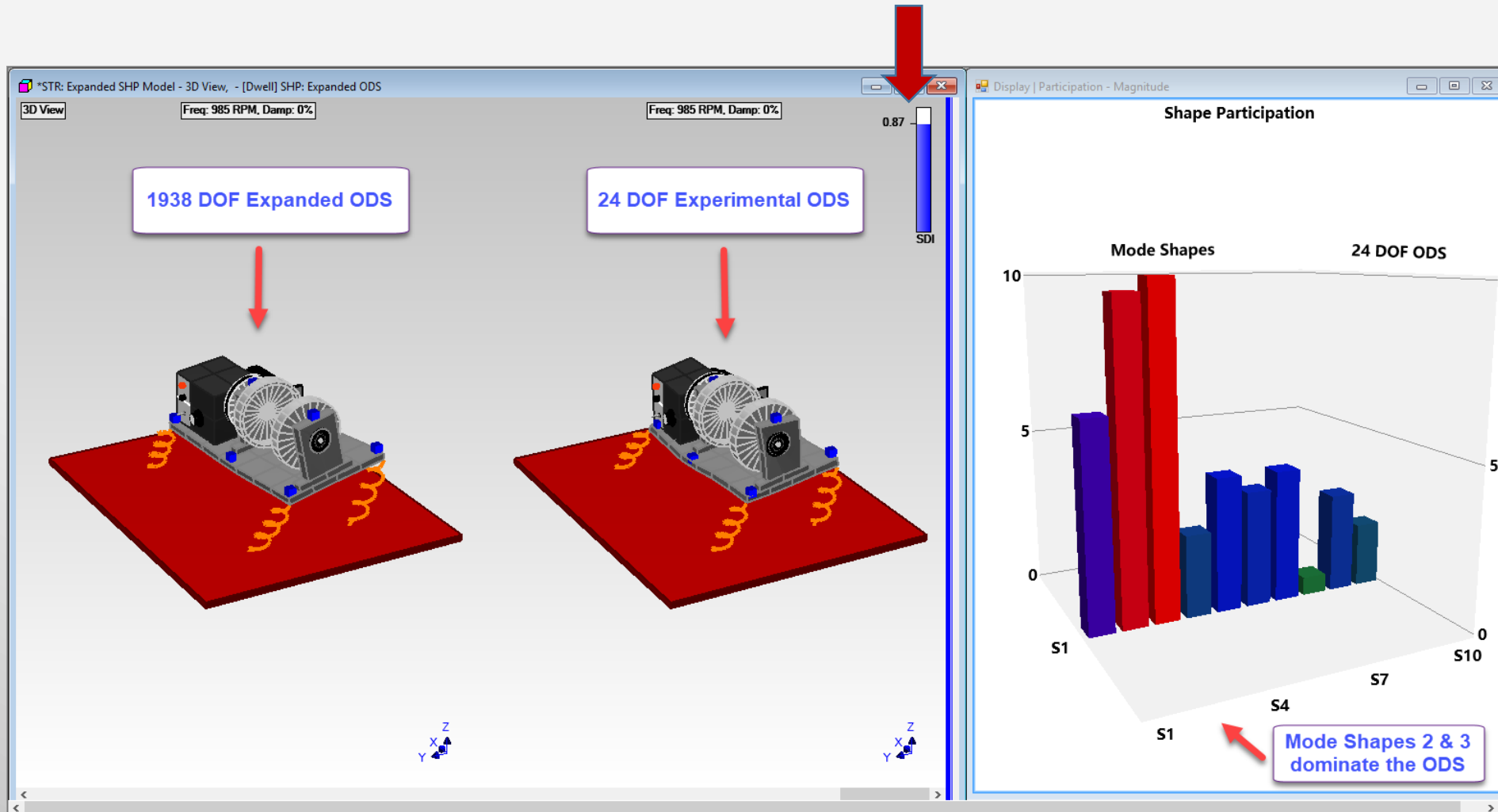
*Numerical comparison between two shapes*

- $SDI = 1 \rightarrow$  two shapes are *the same*
- $SDI > 0.9 \rightarrow$  *almost the same*
- $SDI < 0.9 \rightarrow$  *not the same*

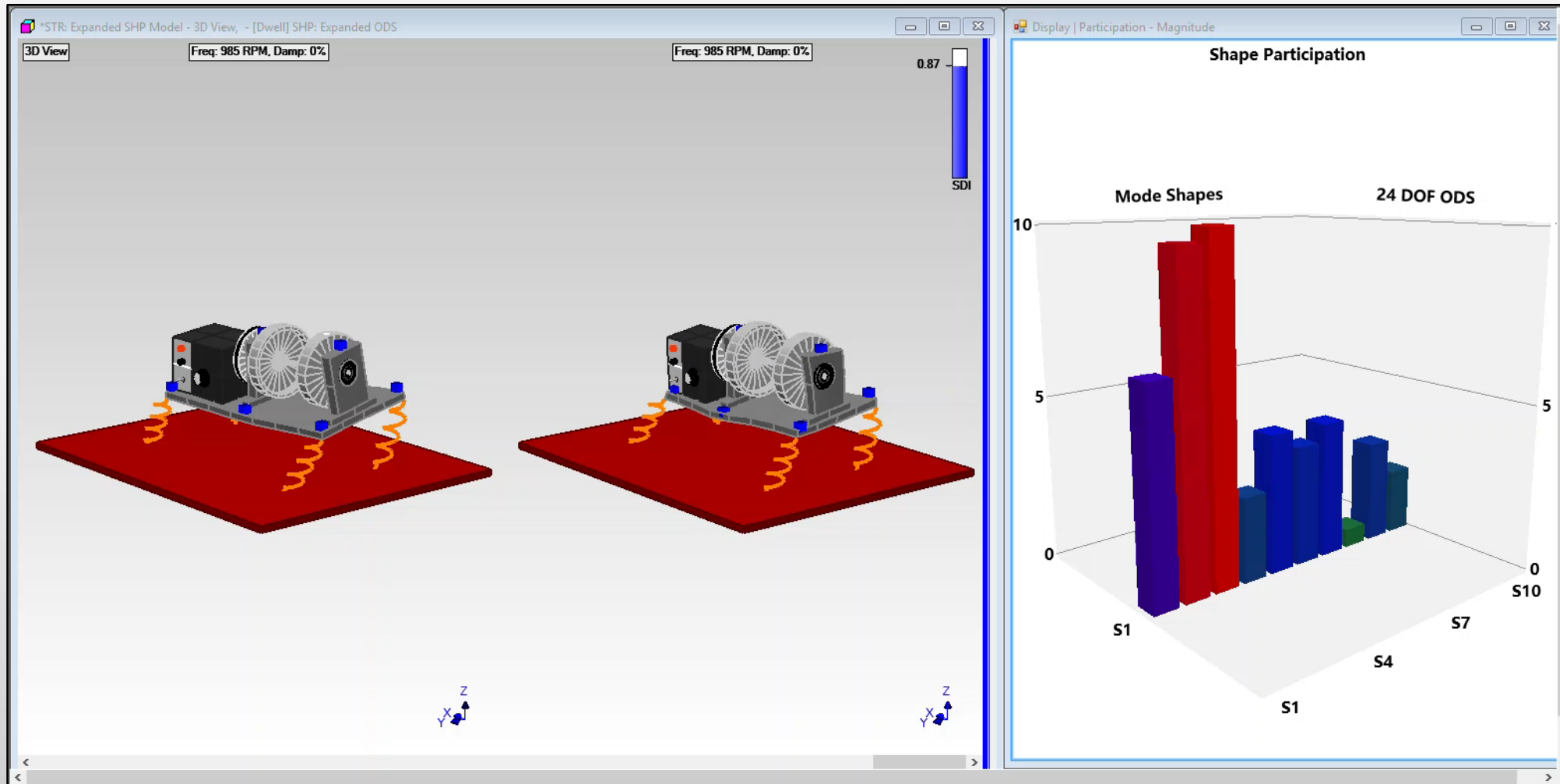


# Mode Shape Participation in the ODS at 985 RPM

The *high SDI value (0.87)* verifies that the *ODS is accurately represented as a summation of mode shapes*



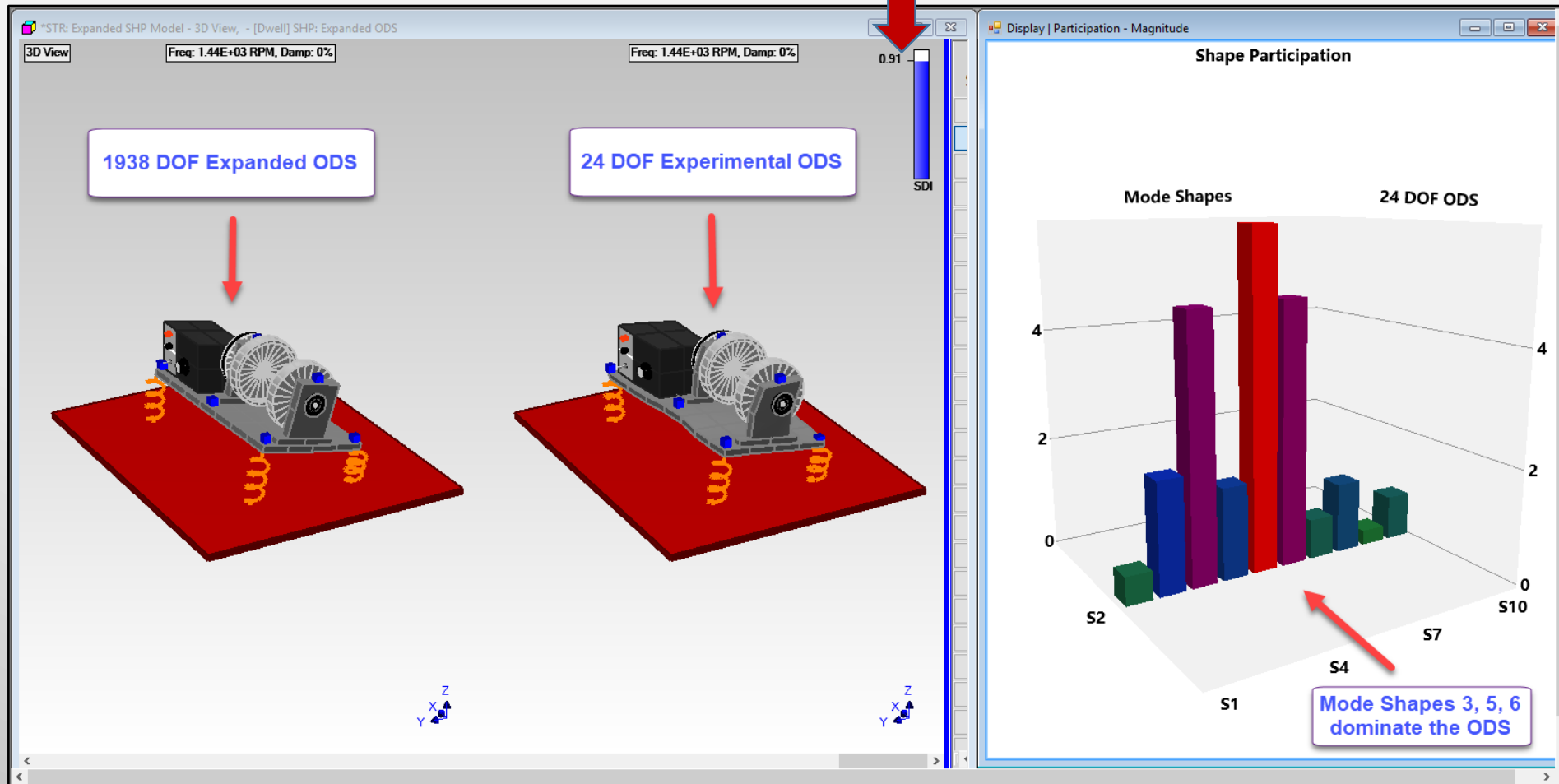
# Mode Shape Participation in the ODS at 985 RPM



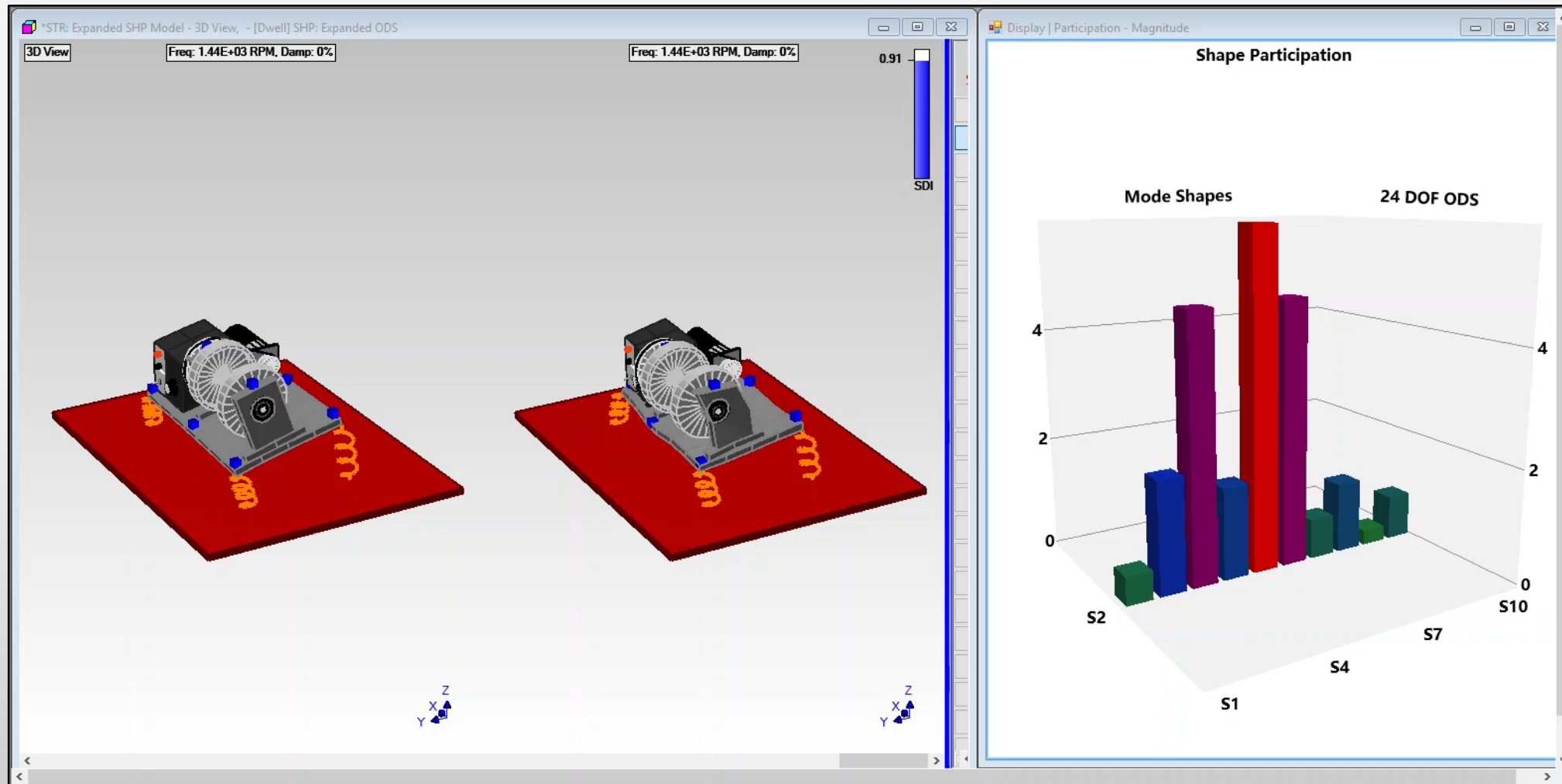
Video

# Mode Shape Participation in the ODS at 1440 RPM

The *high SDI value (0.91)* verifies that the *ODS is accurately represented* as a *summation of mode shapes*



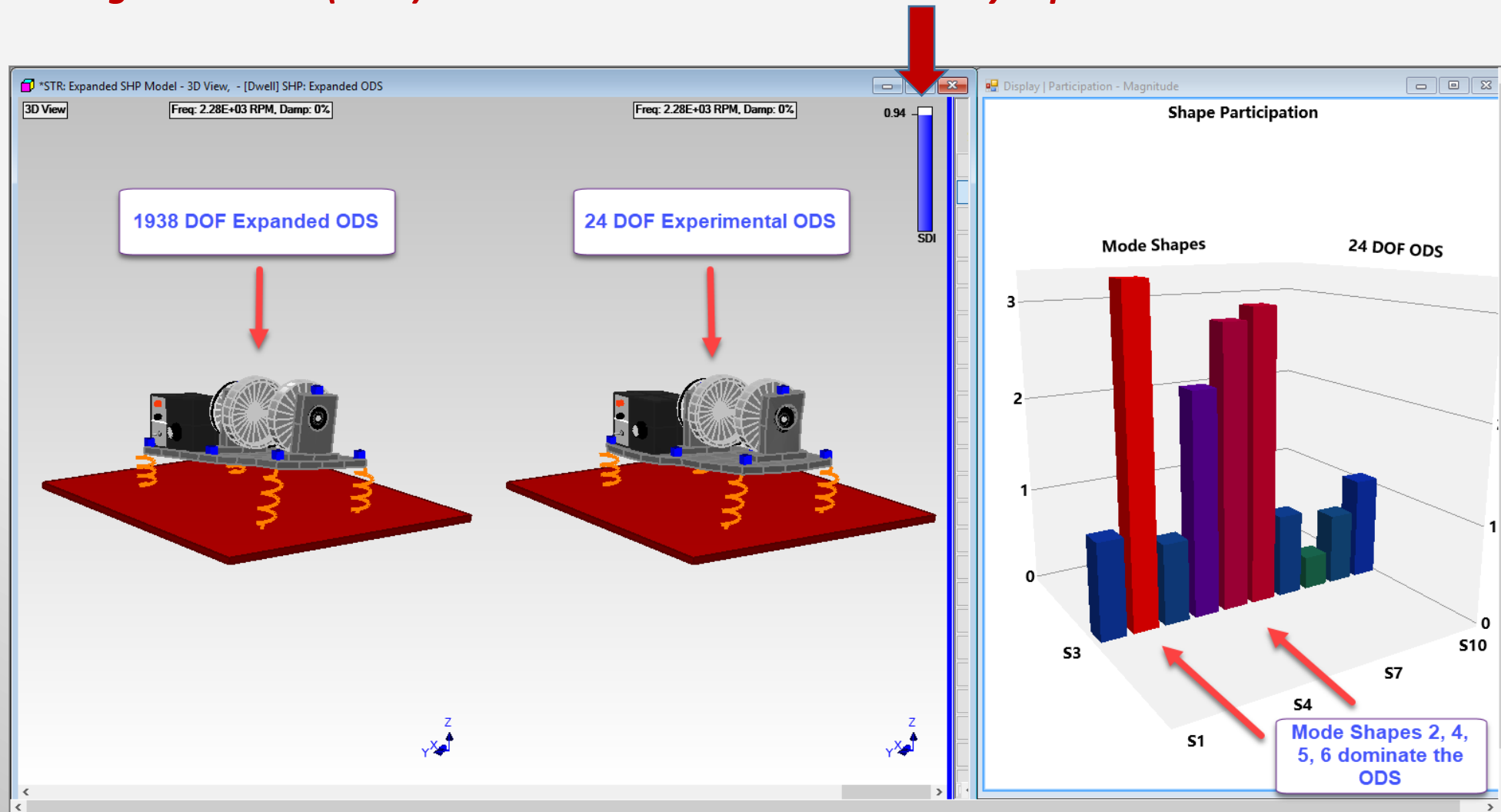
# Mode Shape Participation in the ODS at 1440 RPM



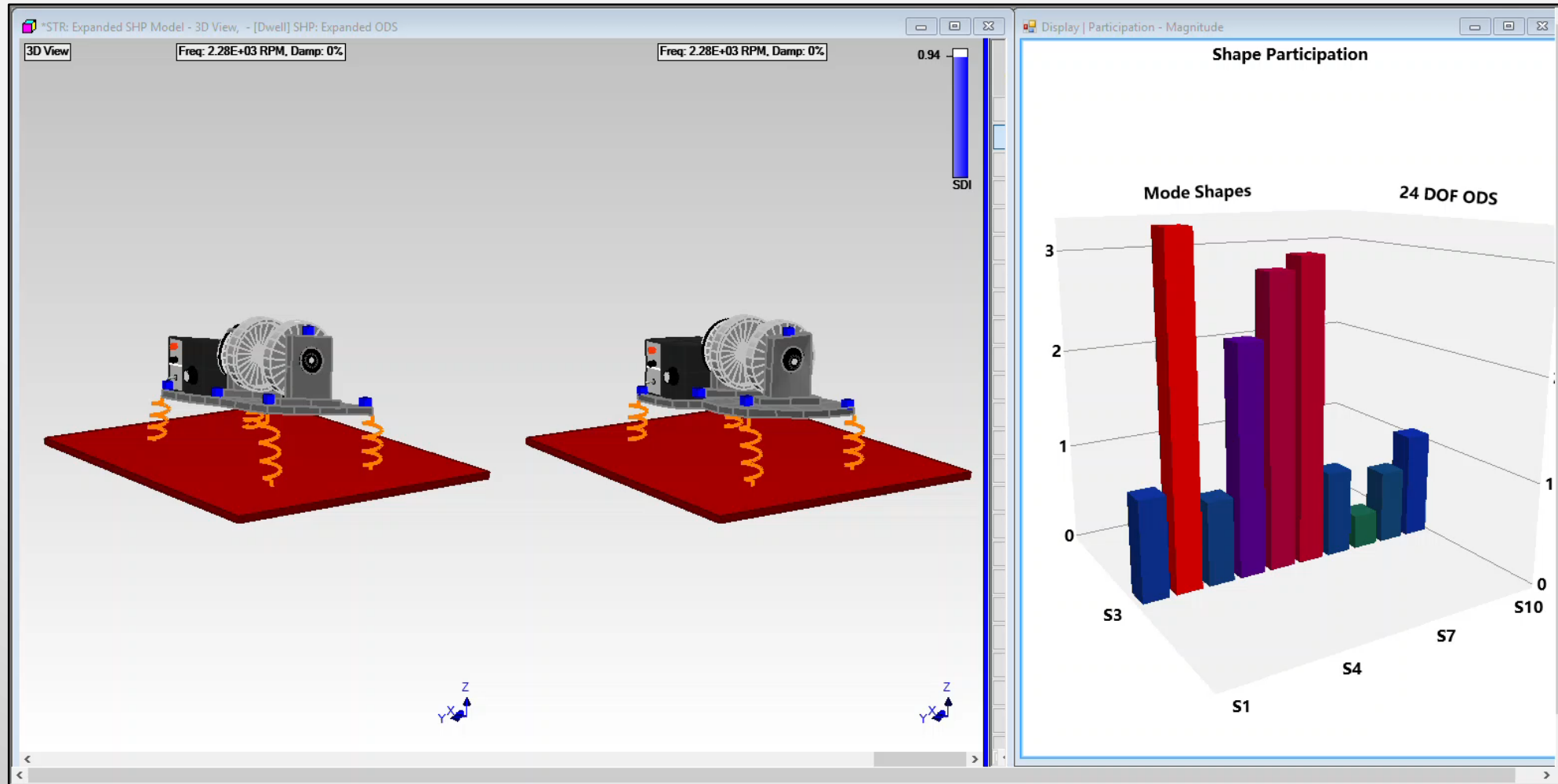
Video

# Mode Shape Participation in the ODS at 2280 RPM

The *high SDI value (0.94)* verifies that the *ODS is accurately represented as a summation of mode shapes*



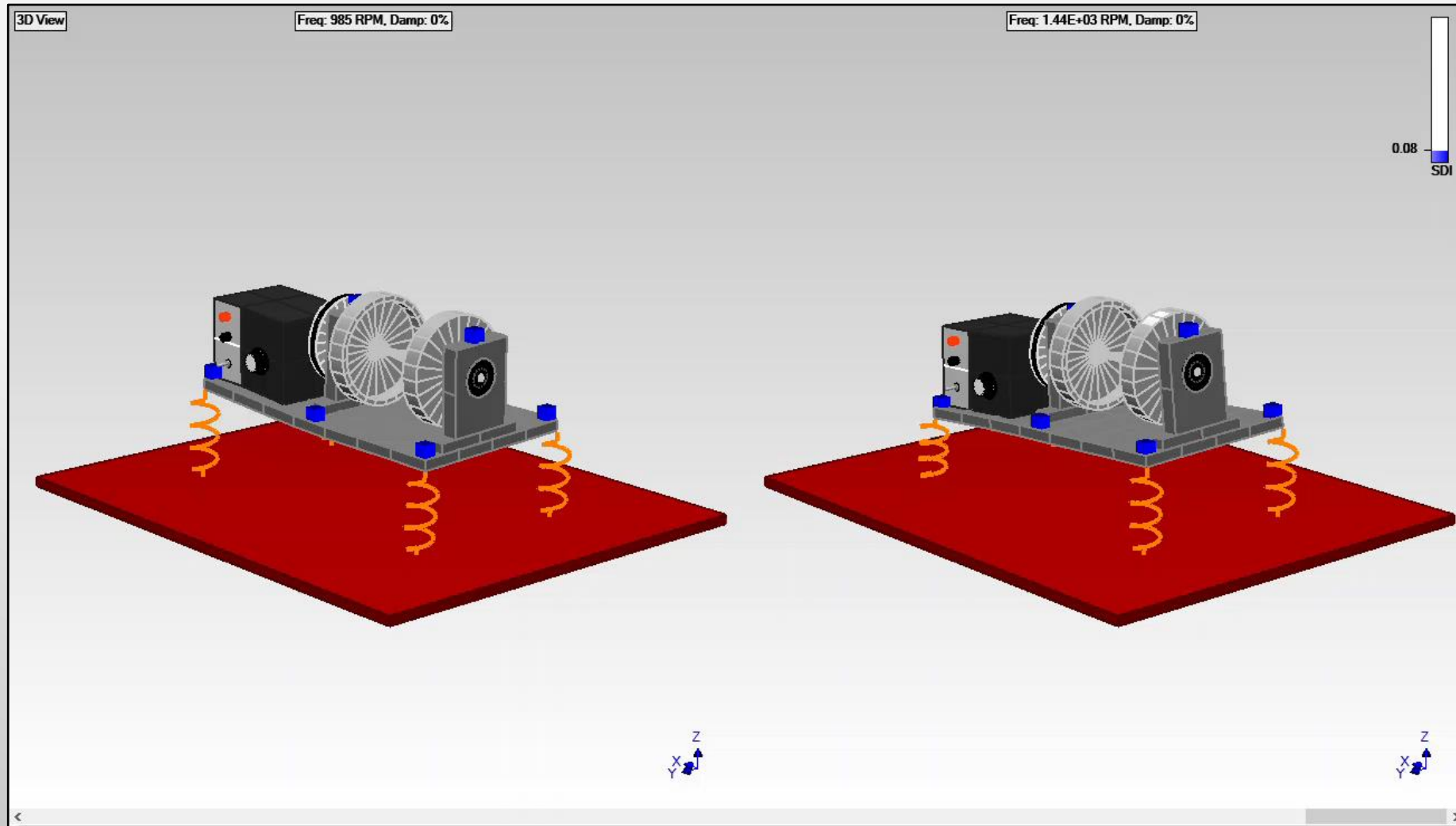
# Mode Shape Participation in the ODS at 2280 RPM



Video

# 985 RPM versus 1440 RPM ODS

The *low SDI value (0.08)* indicates that these two Deflection Shapes are *very different*

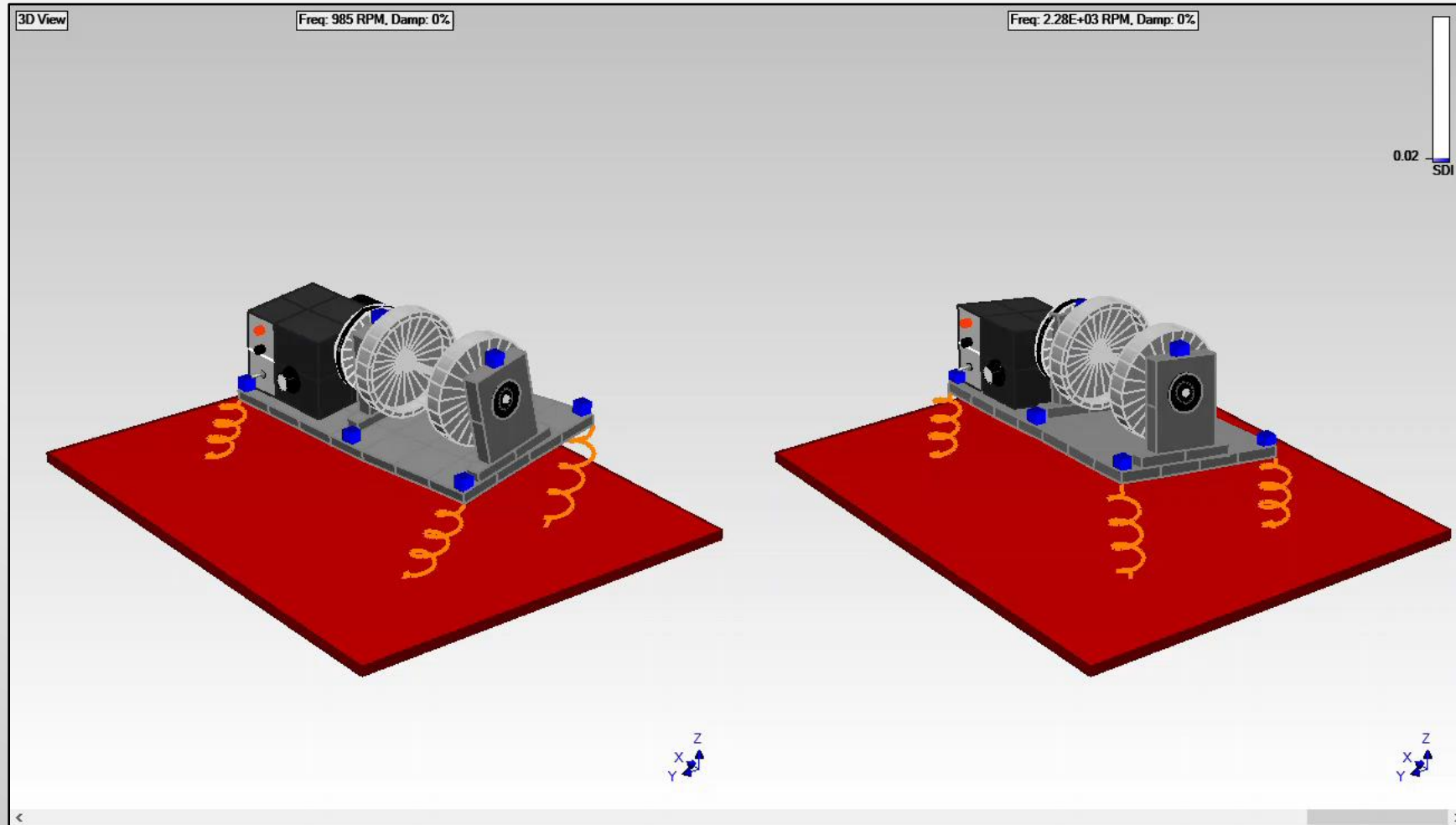


Video



# 985 RPM & 2280 RPM ODS

The *low SDI value (.02)* indicates that these two Deflection Shapes are *very different*



Video

# ODS's versus Mode Shapes

## ODS's

1. ODS's are *defined at any frequency or at any time value*
2. If the *forces or loads change* on a structure, its *ODS's change*
3. Each ODS is a *summation of mode shapes*

## Mode Shapes

1. Mode shapes are *defined at specific natural frequencies*
2. If the *forces or loads change* on a structure, its mode shapes *don't change*
3. EMA mode shapes are *extracted from ODS data*

# ODS's versus Mode Shapes

## ODS's

- 4. ODS's *have engineering units*
- 5. ODS's *have unique values*
- 6. An ODS *defines the actual motion* of each DOF
- 7. ODS's change if the *material properties* or *boundary conditions* or *excitation forces* change

## Mode Shapes

- 4. Mode shapes *don't have engineering units*
- 5. Mode shapes *don't have unique values*
- 6. A mode shape *defines the relative motion* between two DOFs
- 7. Mode shapes change if the *material properties* or *boundary conditions* change

# Summary

- All vibration is *caused by applied forces*
  - Forces *are measured* during an *impact or shaker modal test*
  - Forces *are not measured* during an *ODS test* of an operating machine
- All modes *participate in all vibration*
  - First Law of Modal Analysis (1<sup>st</sup> LoMA): *Any object with mass & elasticity will vibrate*
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